

# Analytically Driven Power Distribution Applications

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- Overview
- Problem Formulations
- Example Applications
- Remarks
- Discussion

Terrestrial Distribution Systems

[[power.ece.drexel.edu](http://power.ece.drexel.edu)]

**DOE, NSF, Utilities, Vendors**



Space Power Systems

[[www.nasa.gov](http://www.nasa.gov)]

Hybrid Electric Cars/Vehicles

[[www.honda.com](http://www.honda.com)]

**Industry**

Shipboard Power Systems

[[www.navyleague.org](http://www.navyleague.org)]

**ONR**

- **Properties:**

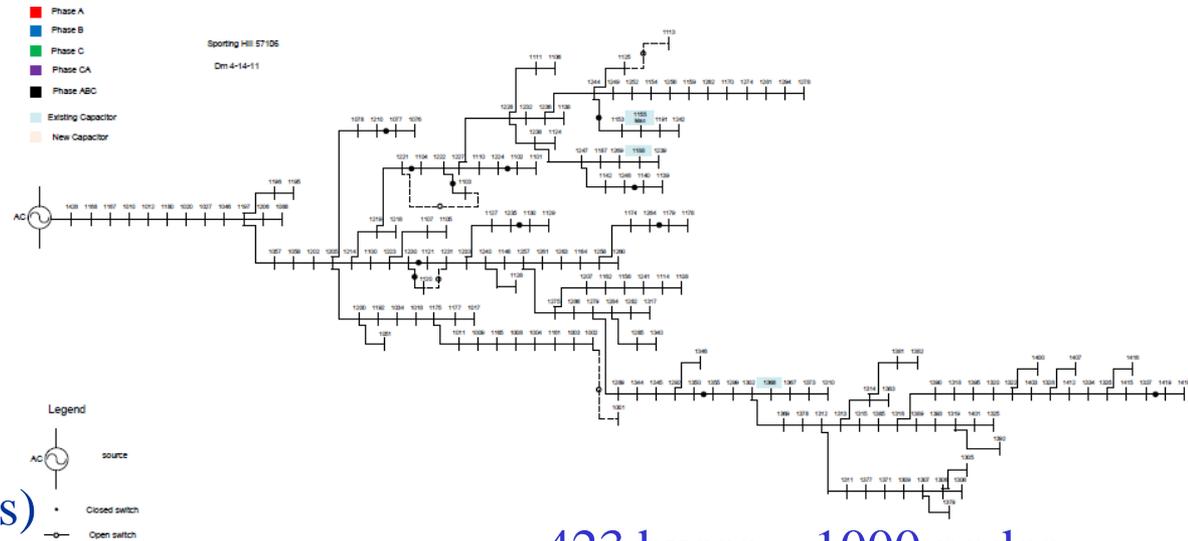
- large systems  
(10,000+ nodes)

- normally operated in a radial manner

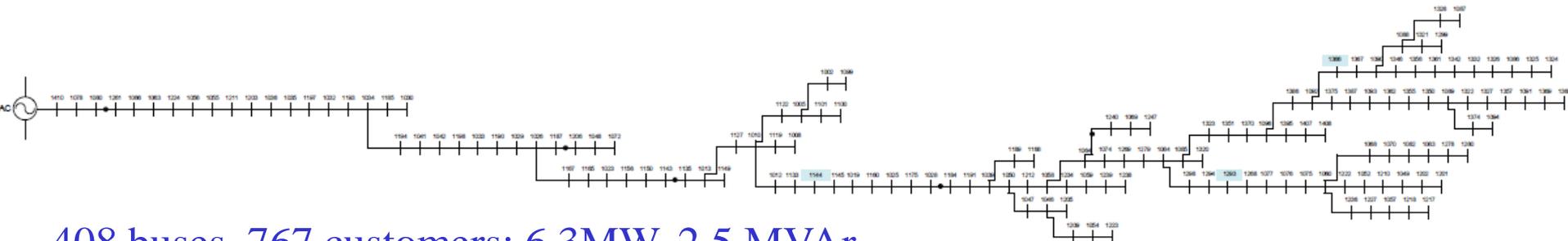
(embedded switches for loops)

- limited # of real-time measurements

- uncertainty of loads and generation (stochastic)



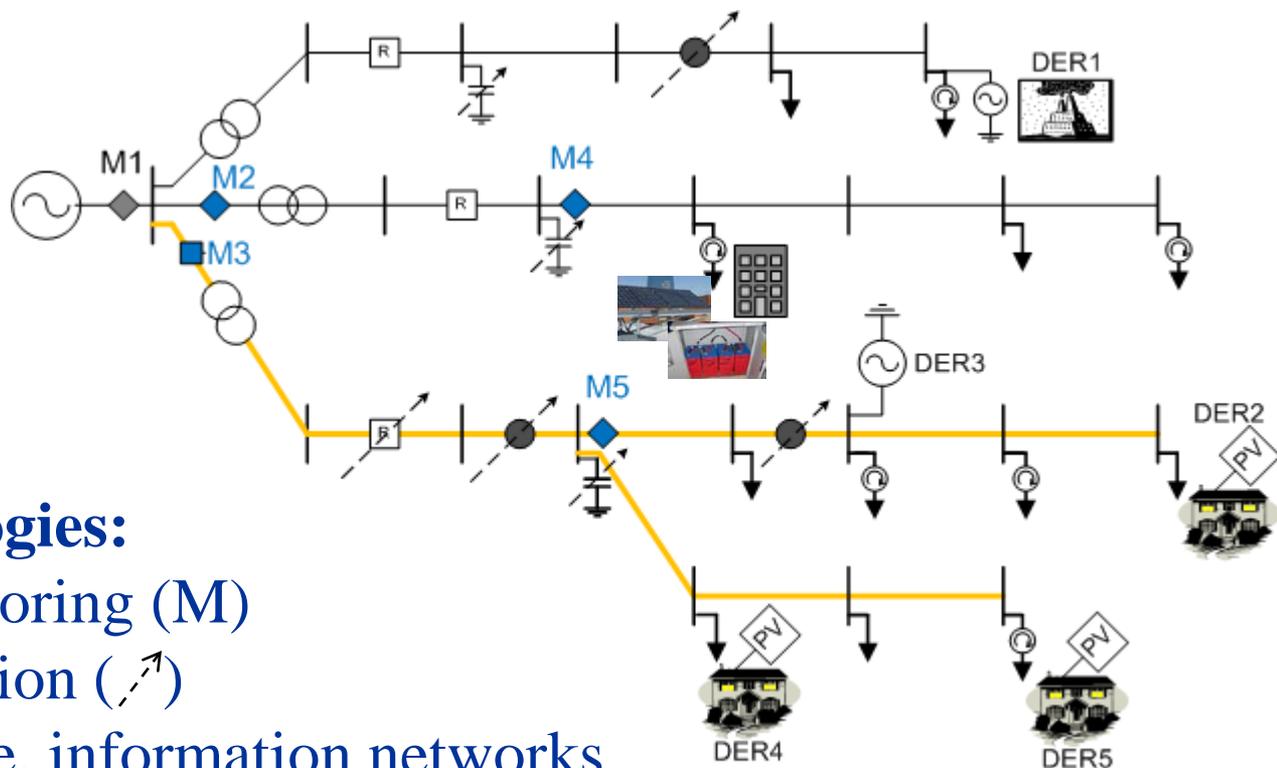
423 buses, ~1000 nodes,  
842 customers: 5.6MW, 1.2 MVar  
(only 3 phase buses drawn)



408 buses, 767 customers: 6.3MW, 2.5 MVar  
(only 3 phase buses drawn)

- **U.S. Properties:**

- multi-phase: 2, 3, 4 and 5-wire systems
- grounded and ungrounded
- above ground and underground
- large



- **Enabling technologies:**

- advanced monitoring (M)
- control automation (↗)
- cost manageable, information networks

- Specific Functions of Distribution Automation
- Examples
  - Objective: Improve Reliability
    - Application = Network Reconfiguration/Service Restoration
  - Objective: Improve Efficiency
    - App. = Network Reconfiguration/Load Balancing
    - App. = Voltage/VAR Control (CVR)
  - Objective: Peak Load Management
    - App = Voltage/VAR Control
    - App = Demand Side Management

- Overview
- Technical Approach
- Example Applications
- Remarks
- Discussion

- **Unbalanced component and system analysis tools**
- **Problem Formulations (focus)**
  - planning: optimal placement and replacement/retrofit
    - economically (\$) driven
  - operation: control of new technologies
    - customer driven
    - shortened time-windows
- **Solution Algorithms**
  - heuristics
    - Expert system & analytically-based
    - Metaheuristics (intelligent system)
  - mathematical programming (require model/formulation simplifications)

- **Examples**
  - Switch Placement & Control for Service Restoration
  - Capacitor Placement & Control for Voltage Spread Reduction
- Optimization ( $C$ : objectives)
  - $F$ : Electrical network constraints (equality)
  - $G$ : Operating constraints (inequality)

$$\min_{u \in U} C(x, \lambda, u)$$

*s.t.*

$$F(x, \lambda, u) = 0$$

$$G(x, \lambda, u) \leq 0$$

– where

- $x$ : states ( $\theta, |V|$ );  $\lambda$ : parameters (uncontrollable loads);  $u$ : control variables (generation/loads, network device status)
- $U$  is the search space

- Switch Placement

Table: Select Goals Considered for Switch Placement Problems

Consideration	Impact/Metric
Field Limitations	$U$ , search space, reduced
Regulatory: e.g. CAIFI	Customer count between switches
SAIFI: Load Restored	Transfer capability of switches
Load Variations (e.g. Cold-Load Pickup)	“ Load curtailment capability

Note:

- analytically determined values are shaded green
- to account for loads, analysis will be necessary
- $U$ : gang-operated switches between any two 3P buses

- Switch Placement

Table: Select Constraints for Switch Placement Problems

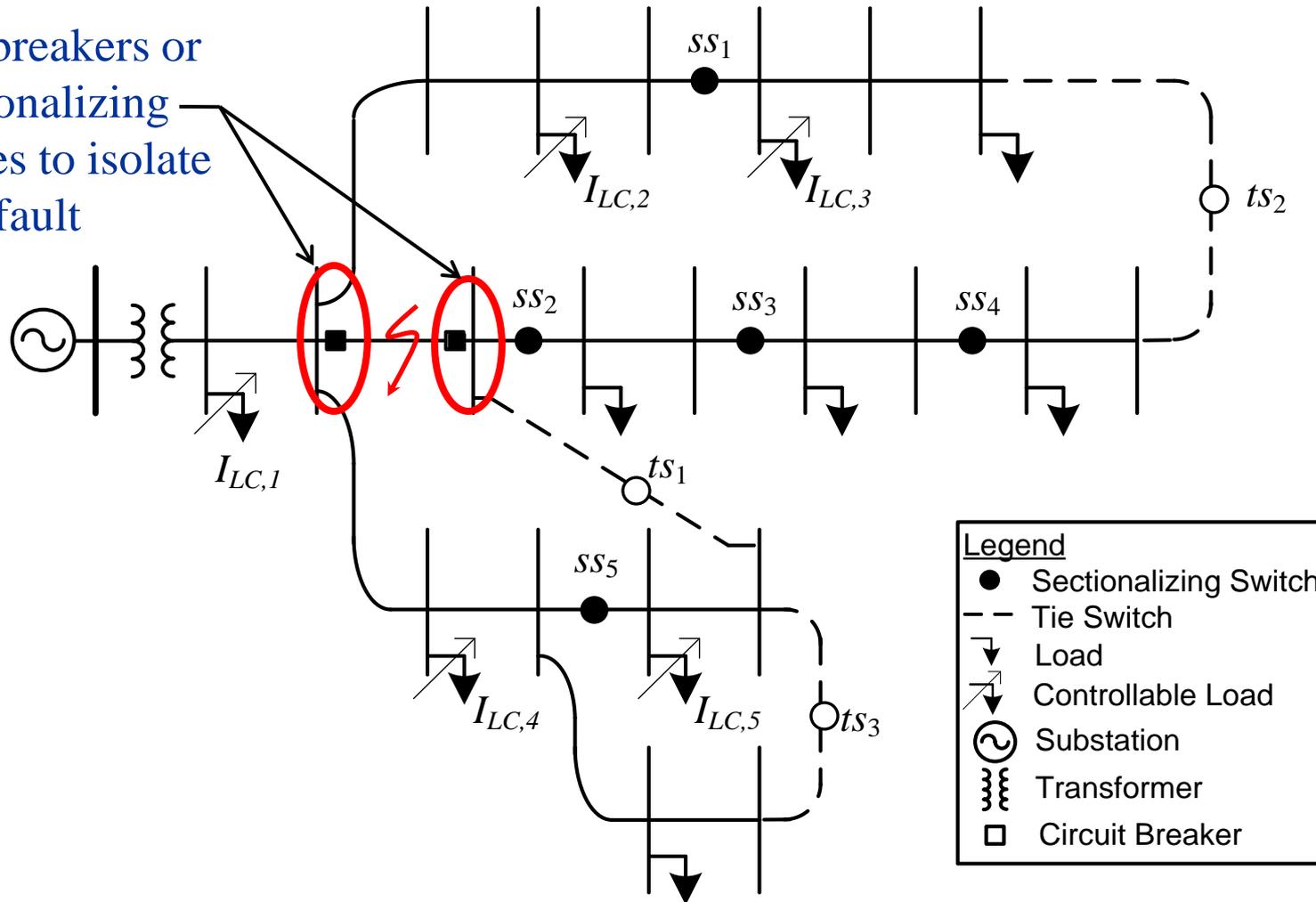
Consideration	Constraint
Voltage Magnitude	$V_k^{p,\min} \leq V_k^p \leq V_k^{p,\max}$
Current Magnitudes	$I_k^p \leq I_k^{p,\max}$
Power Flows	$S_k^p \leq S_k^{p,\max}$
Voltage Rise	$\left   V_k^p(u^{exist})  -  V_k^p(u^{new})  \right  \leq \Delta V_k^{p,\text{rise}}$
Switch Voltage	$ V_i^p  -  V_k^p  \leq \Delta V_{ik}^{p,\max} \quad \forall \text{switches (conn. bus } i \text{ to } k)$

– Note: all analytically determined values

- Switch Placement
  - if based only on non-analytical indices (e.g. *customer count*) reduces flexibility of operations when considering load variations (e.g. *cold-load pick-up*)
  - transfer capability can be adjusted to account for forecasted load variations
- Switch Control
  - What if the switches are already in place?
    - Analytically based approaches can assist
    - Load control/curtailment may be invoked if available  
e.g. [M. Kleinberg et. al. to appear – TPWRS.2010.2080327]
    - Distributed resources may also be considered  
e.g. [Y. Mao et. al. 2003 - TPWRS]

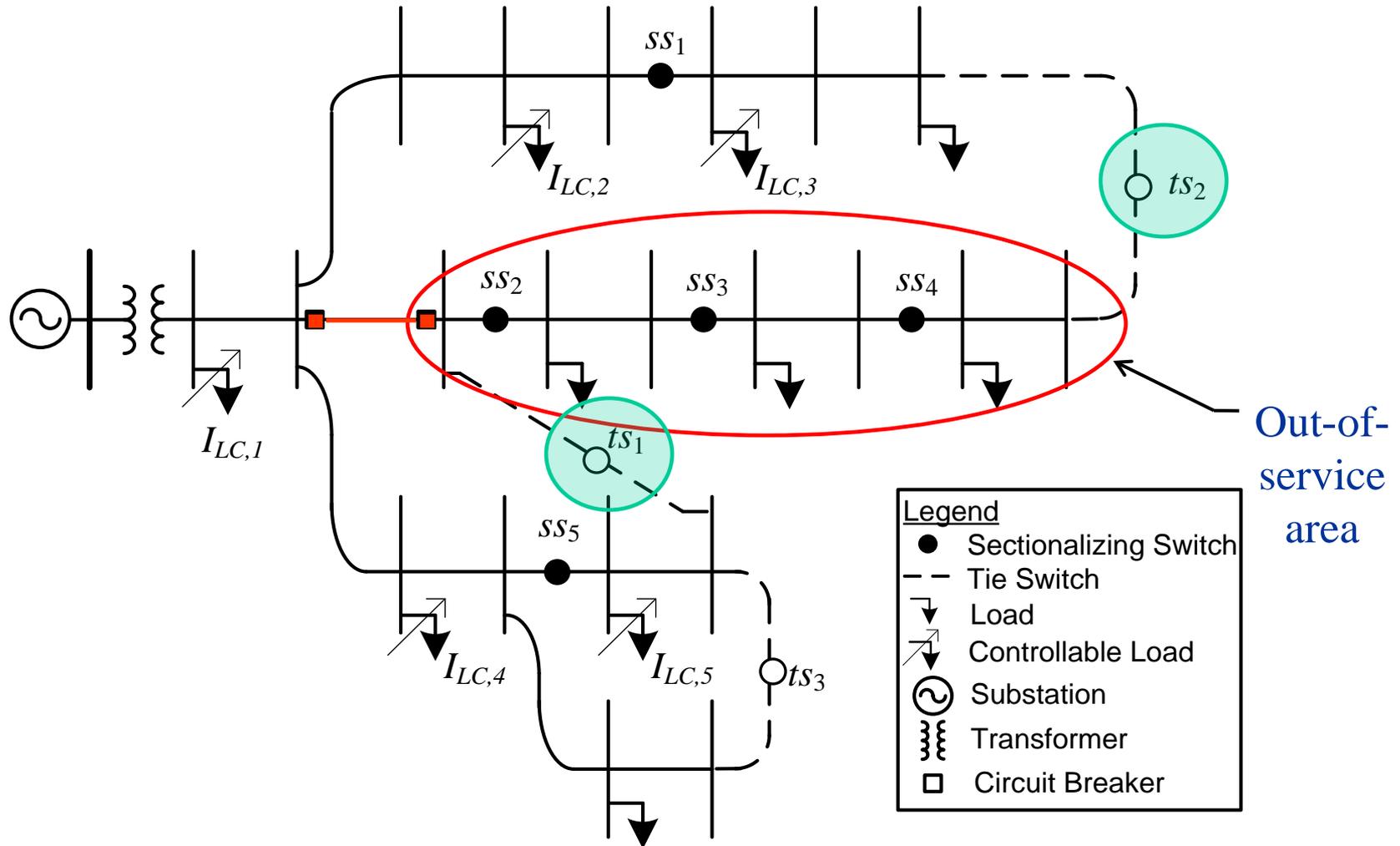
## Service Restoration with Load Curtailment

Open breakers or sectionalizing switches to isolate fault



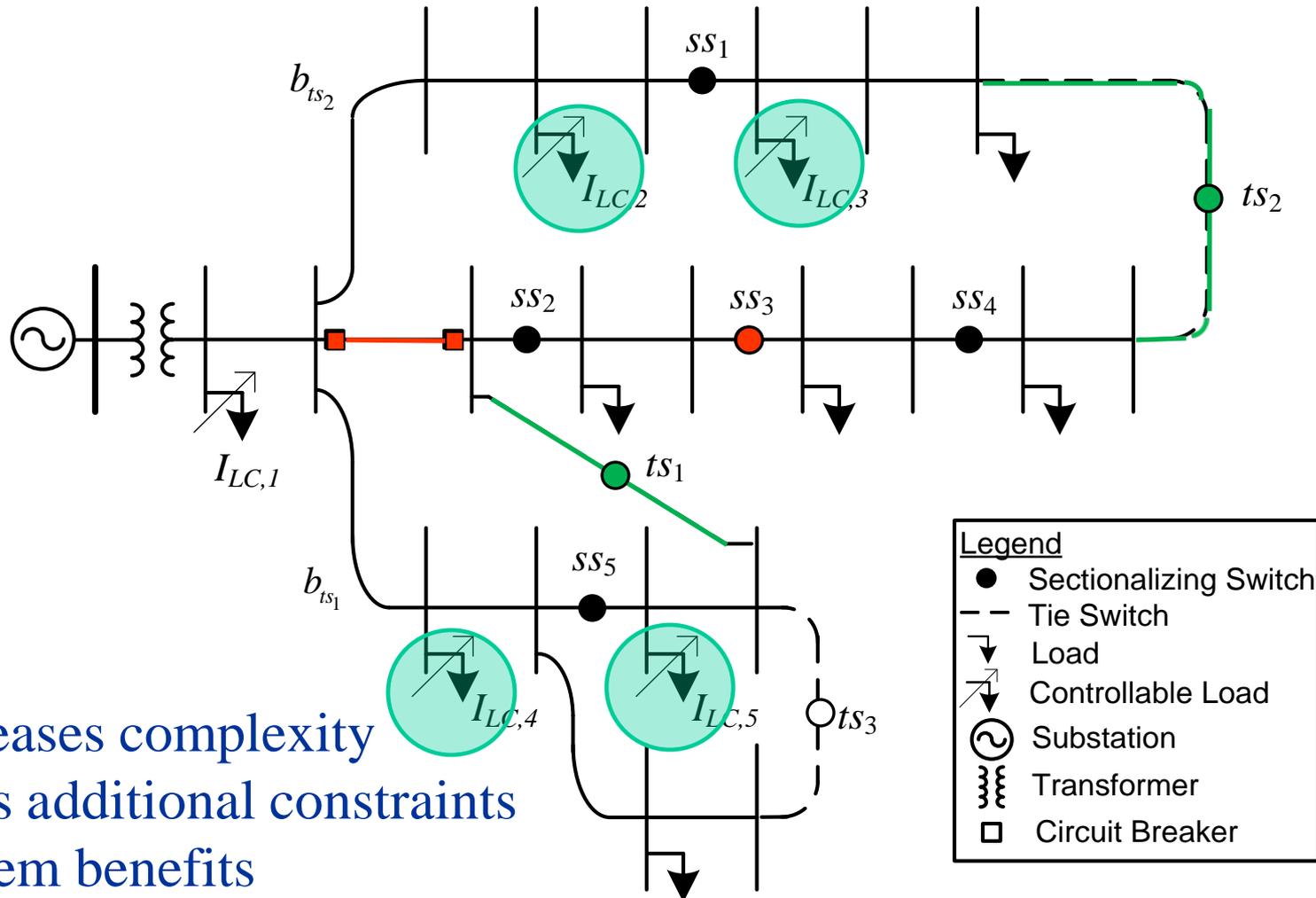
Breakers or sectionalizing switches operated to isolate faulted area

## Service Restoration with Load Curtailment



Traditional restoration schemes limited by network spare capacity

## Service Restoration with Load Curtailment



- Increases complexity
- Adds additional constraints
- System benefits

Load curtailment may be used to free-up additional capacity

- **Examples**
  - Switch Placement & Control for Service Restoration
  - Capacitor Placement & Control for Voltage Spread Reduction
- Optimization ( $C$ : objectives)
  - $F$ : Electrical network constraints (equality)
  - $G$ : Operating constraints (inequality)

$$\begin{aligned} & \min_{u \in U} C(x, \lambda, u) \\ & s.t. \\ & \quad F(x, \lambda, u) = 0 \\ & \quad G(x, \lambda, u) \leq 0 \end{aligned}$$

– where

- $x$ : states ( $\theta, |V|$ );  $\lambda$ : parameters (uncontrollable loads);  $u$ : control variables (generation/loads, network device status)
- $U$  is the search space

- Capacitor Placement

Table: Goals Considered for Capacitor Placement Problems

Consideration	Impact/Metric
In-Field Physical Space	$U$ , search space, reduced
Regulatory: Peak Load Reduction	Substation voltage and PQ
System Voltage Spread	Node voltages
System Loss Levels	Branch flows/losses

Note:

- analytically determined values are shaded green
- $U$ : all 3P buses, included sizing of existing capacitors

- Capacitor Placement

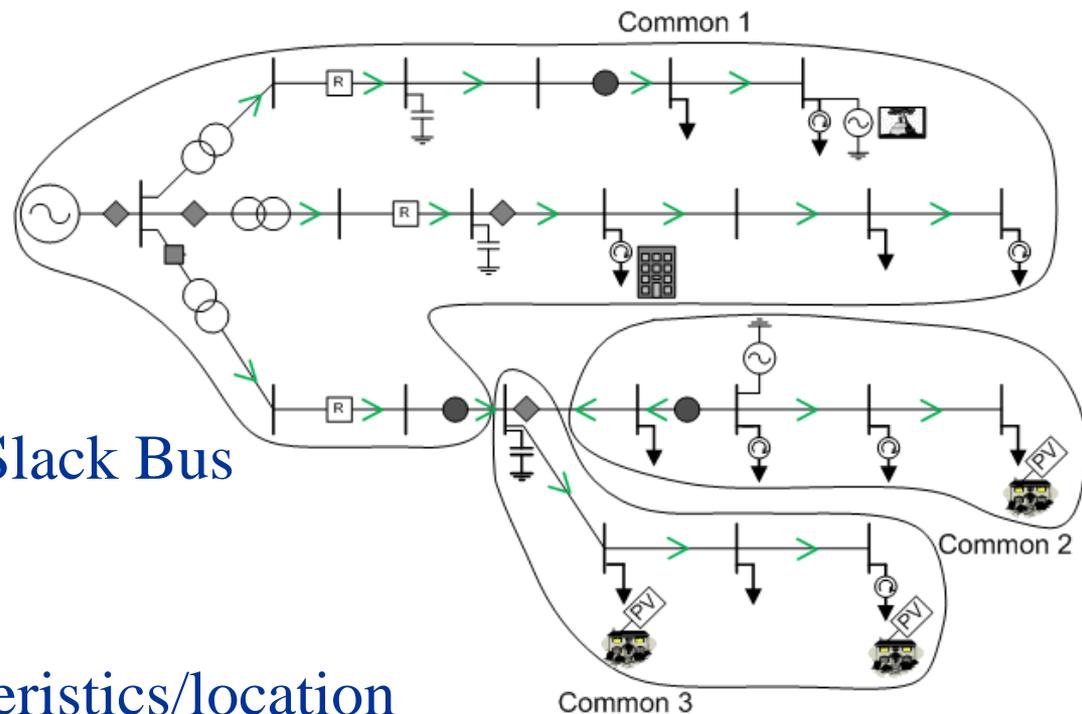
Table: Constraints for Capacitor Placement Problems

Consideration	Constraint
Voltage Magnitude	$V_k^{p,\min} \leq  V_k^p  \leq V_k^{p,\max}$
Current Magnitudes	$ I_k^p  \leq I_k^{p,\max}$
Power Flows	$ S_k^p  \leq S_k^{p,\max}$
Voltage Rise	$\left   V_k^p(u^{exist})  -  V_k^p(u^{new})  \right  \leq \Delta V_k^{p,\text{rise}}$
Substation Power Factor	$Q_{sub}^{\min} \leq  Q_{sub}^{total}  \leq Q_{sub}^{\max}$

– Note: all analytically determined values

- Capacitor Placement
  - Priority of objectives should be adjusted wrt load levels.
    - Example to include: peak, 70% loading and low load levels
  - Introducing different levels of analytics yields different results
    - Examples:
      - With power factor constraints and without
      - With system loss considerations and without
- Capacitor Control
  - # of load levels considered will impact operations
  - time windows vary wrt voltage spread vs. loss reduction
  - constraints are also time dependent: e.g. **maximum number of switch operations** within a 24 hr period.

- Practical Field Limitations – reduce the search space
- Operator Preferences
  - controller proximity
- Create directed graphs
- Domain-Based Distributed Slack Bus Models ( $P$  graphs)
  - attribute load and losses
  - considers network characteristics/location



Energy resource power domains/commons

- Domain-Based Capacitor Placement ( $Q$  graphs)
  - considers the location of other capacitors
  - enables “physical spread” of caps

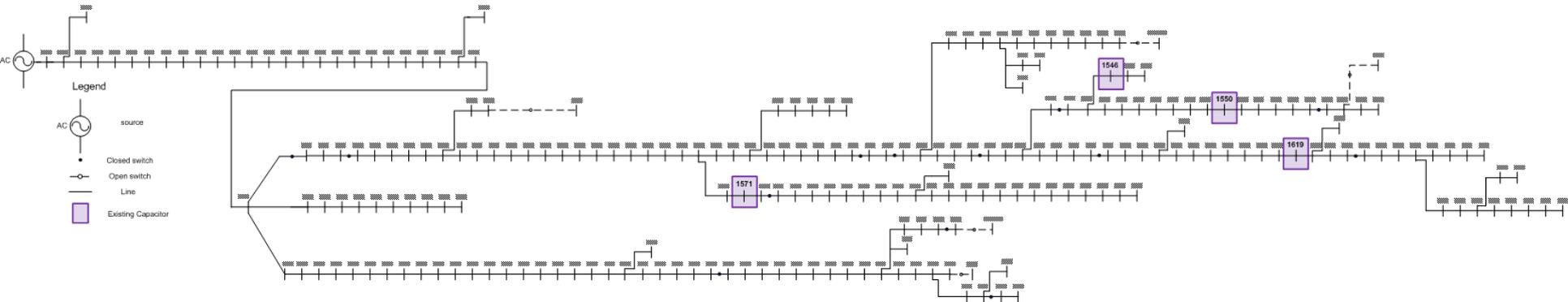
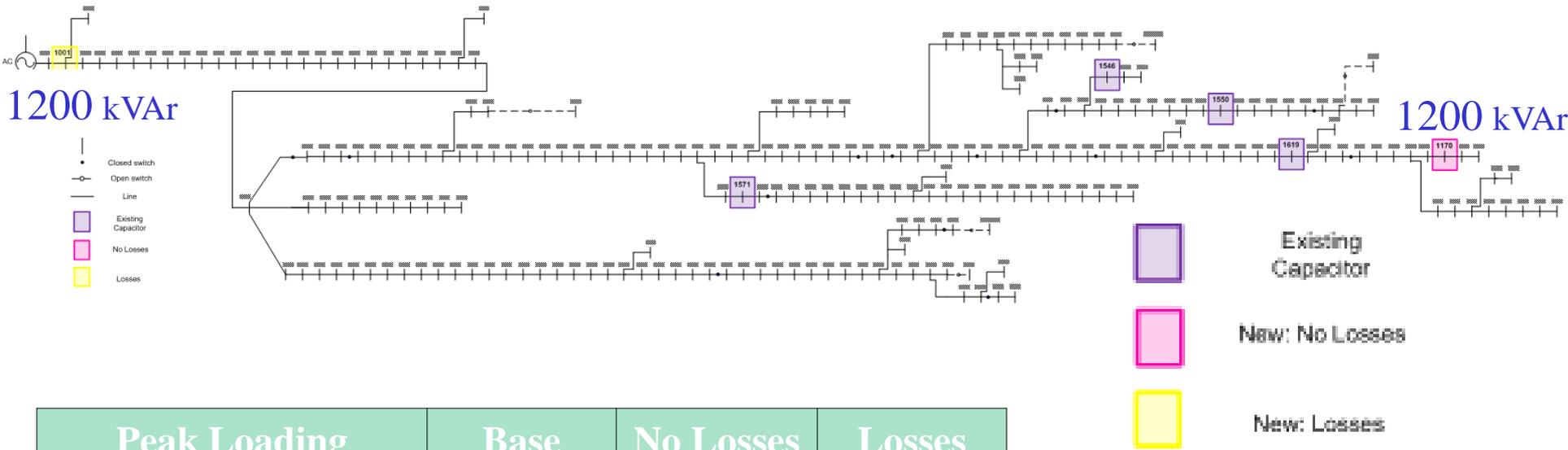


Figure: One-Line Diagram of a 690 bus system

Electrical Component	Count
# of Buses	690
# of Nodes	1082
# of Customers	1864
# of Loads	365
# of 3-Phase Buses	245
3-Phase Capacitors	4

Substation	Quantity
Total $P_{Load}$ (kW)	5553
Total $Q_{Load}$ (kVAr)	1753

Bus Number	Size (kVAr)	Cap Type
1546	900	Automated
1550	600	Automated
1619	900	Automated
1571	600	Manual



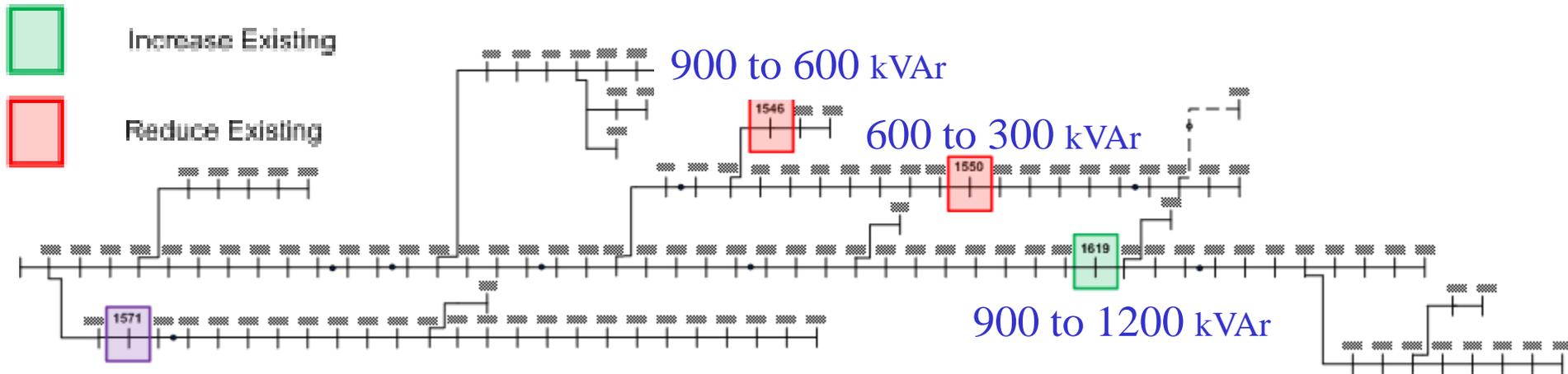
Peak Loading	Base case	No Losses	Losses
V  spread (p.u.)	0.0317	0.0214	0.0314
Substation Q (kVAr)	-895.83	-2100.33	-2089.77
Substation Power Factor (PF)	0.9879 leading	0.9393 leading	0.9392 leading
Total $P_{Loss}$ (kW)	164.55	199.58	165.129

Selected  $u$ :

- Different cap placement
- Increased substation Q

Resulting metrics:

- Voltage spread decreased
- $P_{loss}$  increased
- Substation PF decreased



Peak Loading	Base case	No Losses	Losses
V  spread (p.u.)	0.0317	0.0337	0.0337
Substation Q (kVAr)	-895.83	-599.73	-599.73
Substation Power Factor (PF)	0.9879 leading	0.9945 leading	0.9945 leading
Total $P_{Loss}$ (kW)	164.55	160.85	160.85

Selected  $u$ :

- Identical cap placement
- Reduced substation Q

Metrics:

- Voltage spread increased
- $P_{Loss}$  decreased
- Substation PF increased

- Analytically driven applications broaden the scope and scenarios under study.
- Practical considerations should be leveraged to reduce problem size and complexity (as well as facilitate acceptance of results.)
- Each distribution circuit has its own properties/characteristics
  - With measurements, this can be quantified; hence, modeled.
- As a result, systematic, repeatable approaches to distribution circuit planning and operation can be realized and used as a guide for engineers.

- Remaining Challenges
  - Access to Power Engineering Education
    - Relatively few universities with power programs
    - Fewer have formal education in power distribution systems
  - We do not have a baseline
    - Economically driven investments require an accepted baseline
  - Technical challenges
    - Impacts of large numbers of new components
    - Time and space scaling issues
    - Real-time operation with unsynchronized measurements
    - Large-scale, mixed-integer optimization problems